

Melani A. Situmorang

Professor In Hak Moon

MATH101RO - College Mathematics

April 6, 2020

Find each sum, difference, and product:

#2. $(4m^3 - 3m^2 + 5) + (-3m - m^2 + 5) =$

Answer:

$$4m^3 - 3m^3 - 3m^2 - m^2 + 5 + 5 = m^3 - 2m^2 + 25$$

#4. $(8p^2 - 5p) - (3p^2 - 2p + 4) =$

Answer:

$$8p^2 - 3p^2 - 5p - 2p + 4 = 5p^2 - 7p + 4$$

#6. $-(8x^3 + x - 3) + (2x^3 + x^2) - (4x^2 + 3x - 1) =$

Answer:

$$-8x^3 + 2x^3 + x^2 - 4x^2 + x + 3x - 3 - 1 = -6x^3 + 3x^2 + 4x - 4$$

#8. $8x^2y - 3xy^2 + 2x^2y - 9xy^2 =$

Answer:

$$8x^2y + 2x^2y - 3xy^2 - 9xy^2 = 10x^2y - 12xy^2$$

#10. $(y-3) \cdot (y-9) =$

Answer:

Distribute and multiply them.

$$(y \cdot y) (y \cdot 9) (-3 \cdot y) (-3 \cdot 9) =$$

$$y^2 - 9y - 3y - 27 = y^2 - 12y - 27$$

#12. $(5m - 6) \cdot (3m+4) =$

Distribute and multiply them

$$(5m \cdot 3m)(5m \cdot 4)(-6.3m)(-6.4) = 15m^2 + 20m - 18m - 24$$
$$= 15m^2 + 2m - 24$$

$$14. 2b^3(b^2 - 4b + 3) =$$

Answer:

$$2b^3(b^2 - 4b + 3) = 2b^5 - 8b^4 + 6b^3$$

$$16. (8s - 3t)(8s + 3t) =$$

Answer:

$$(8s \cdot 8s)(8s \cdot 3t)(-3t \cdot 8s)(-3t \cdot 3t) = 64s^2 + 24st - 24st - 9t^2$$
$$= 64s^2 - 9t^2$$

$$18. (a - 6b)^2 =$$

Answer:

$$(a - 6b)(a - 6b) = a^2 - 6ab - 6ab + 36b^2$$
$$= a^2 - 12ab + 36b^2$$

$$20. (2z^4 - 3y)^2 =$$

Answer:

$$(2z^4 - 3y)(2z^4 - 3y) = (2z^4 \cdot 2z^4)(2z^4 \cdot -3y)(-3y \cdot 2z^4)(-3y \cdot -3y)$$
$$= 4z^8 - 6yz^5 - 6yz^5 + 9y^2$$

$$21. (2z - 1) \cdot (-z^2 + 3z - 4) = 2z^3 + 5z^2 - 11z + 4$$

Answer:

$$z - z^2 + 3z - 4$$

$$2z - 1 \quad \times$$

$$= \quad -z^2 - 3z + 4$$

$$2z^3 + 5z^2 - 8z \quad +$$

$$= 2z^3 + 5z^2 - 11z + 4$$

$$23. (m-n+k) \cdot (m+2n-3k) =$$

Answer:

$$\begin{aligned} & m+2n-3k \\ & m - n + k \quad \times \\ = & 2km+2kn-3k^2 \\ & mn-2n^2+3kn \\ & m^2+mn-3km \quad + \\ = & m^2 + 3mn - km - 2n^2 + 5kn - 3k^2 \end{aligned}$$

$$24. (r - 3s+1) (2r -s+1) =$$

Answer:

$$\begin{aligned} & r - 3s + 1 \\ & 2r - s + 1 \quad \times \\ = & r-3s+1 \\ & rs+3s^2-s \\ & 2r-6rs+2r \quad + \\ = & 2r^2 - 5rs + 3r + 3s - 4s + 1 \end{aligned}$$

$$25. (a+b+2c)^2 = a^2 + 2ab + 4ac + b^2 + 4bc + 4c^2$$

$$a + b + 2c \times a + b + 2c = a^2 + 2ab + 4ac + b^2 + 4bc + 4c^2$$

$$26. (k-y+3m)^2 =$$

Answer:

$$(k-y+3m) \cdot (k-y+3m) = k^2 + 6km + y^2 - ym^2$$

Factor the greatest common factor from each polynomial:

$$32. 2p^5 - 10p^4 + 16p^3 =$$

$$2p^5 = 2 \cdot p \cdot p \cdot p \cdot p \cdot p$$

$$10p^4 = 2 \cdot 5 \cdot p \cdot p \cdot p \cdot p$$

$$16p^3 = 2 \cdot 2 \cdot 2 \cdot 2 \cdot p \cdot p \cdot p$$

$$\text{GCF: } 2 \cdot p \cdot p \cdot p$$

$$\text{GCF: } 2p^3$$

$$= 2p^3 (p^2 - 5p + 8)$$