

HW #1 Math 140

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1. $f(x) = 2x + 4$, $g(x) = 4x^2 + 1$; find $(g \circ f)(0)$

$$(g \circ f)(0) = g(f(0)) = g(4)$$

$$= 4(4)^2 + 1$$

$$f(0) = 2(0) + 4$$

$$= 4$$

$$= 4(16) + 1$$

$$= 64 + 1 = 65$$

D) 65

2. $f(x) = -4x + 9$, $g(x) = 5x + 9$; find $(g \circ f)(x)$

$$(g \circ f)(x) = g(f(x)) = g(-4x + 9)$$

$$= 5(-4x + 9) + 9$$

$$= -20x + 45 + 9$$

$$= -20x + 54$$

B) $-20x + 54$

3. $f(x) = \sqrt{x+8}$, $g(x) = 8x - 12$; find $(f \circ g)(x)$

$$(f \circ g)(x) = f(g(x)) = f(8x - 12)$$

$$= \sqrt{(8x - 12) + 8}$$

$$= \sqrt{8x - 4}$$

$$= \sqrt{4(2x - 1)}$$

$$= 2\sqrt{2x - 1}$$

B) $2\sqrt{2x - 1}$

4. $f(x) = \frac{2}{x-8}$, $g(x) = \frac{5}{8x}$; find $(f \circ g)(x)$

$$(f \circ g)(x) = f(g(x)) = f\left(\frac{5}{8x}\right)$$

$$= \frac{2}{\left(\frac{5}{8x}\right) - 8} = \frac{2}{\frac{5}{8x} - 8}$$

$$\frac{2 \cdot 8x}{\frac{5}{8x} - 8 \cdot 8x} = \frac{16x}{5 - 64x}$$

A) $\frac{16x}{5 - 64x}$

$$5. f(x) = \frac{10}{x+6}$$

$$g(x) = x+10$$

$$f(g(x)) = f(x+10) \rightarrow \frac{10}{(x+10)+6} = \frac{10}{x+16}$$

$$D): x \neq -16$$

indicate whether the function is one-to-one

$$6. \{(-18, 1), (-19, -8), (3, 15)\}$$

yes

7. find the inverse of the function & state its domain and range.

$$\{(-3, 4), (-1, 5), (0, 2), (2, 6), (5, 7)\}$$

$$\text{inverse: } \{(4, -3), (5, -1), (2, 0), (6, 2), (7, 5)\}$$

$$\text{domain: } 4, 5, 2, 6, 7$$

$$\text{range: } -3, -1, 0, 2, 5$$

$$8. f(x) = x^3 + 4$$

$$y = x^3 + 4$$

$$\sqrt[3]{x^3 + 4}$$

$$\sqrt[3]{x-4} = y$$

$$f^{-1}(x) = \sqrt[3]{x-4}$$

$$9. f(x) = \frac{6}{x+4}$$

$$y = \frac{6}{x+4}$$

$$x = \frac{6}{y} - 4$$

$$f^{-1}(x) = \frac{6}{x} - 4$$

$$9. f(x) = \frac{6}{x+4}$$

$$y = \frac{6}{x+4}$$

$$6 = x(y+4)$$

$$6x = y+4$$

$$y = 6x - 4$$

$$f^{-1}(x) = 6x - 4$$

10. graph inverse

inverse function in red



