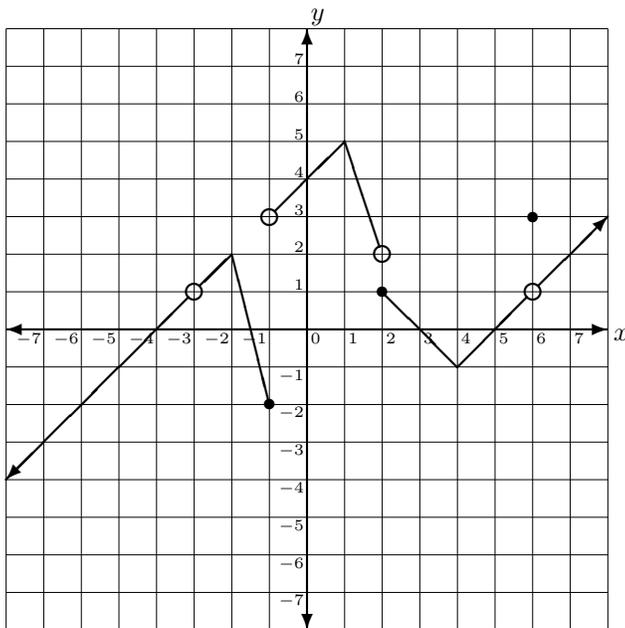


**Example 1.** For the function  $f$  graphed below, find the following:



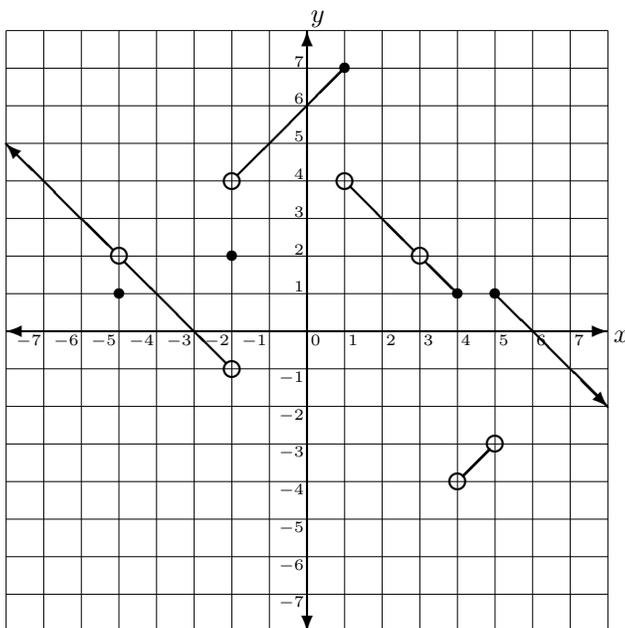
- |                                       |                                       |  |
|---------------------------------------|---------------------------------------|--|
| 1. $\lim_{x \rightarrow -3^-} f(x) =$ | 9. $\lim_{x \rightarrow 2^-} f(x) =$  | 17. $\lim_{x \rightarrow 6^-} f(x) =$                          |
| 2. $\lim_{x \rightarrow -3^+} f(x) =$ | 10. $\lim_{x \rightarrow 2^+} f(x) =$ | 18. $\lim_{x \rightarrow 6^+} f(x) =$                          |
| 3. $\lim_{x \rightarrow -3} f(x) =$   | 11. $\lim_{x \rightarrow 2} f(x) =$   | 19. $\lim_{x \rightarrow 6} f(x) =$                            |
| 4. $f(-3) =$                          | 12. $f(2) =$                          | 20. $f(6) =$   |
| 5. $\lim_{x \rightarrow -1^-} f(x) =$ | 13. $\lim_{x \rightarrow 4^-} f(x) =$ | 21. List the value(s) of $x$<br>at which $f$ is discontinuous. |
| 6. $\lim_{x \rightarrow -1^+} f(x) =$ | 14. $\lim_{x \rightarrow 4^+} f(x) =$ |  |
| 7. $\lim_{x \rightarrow -1} f(x) =$   | 15. $\lim_{x \rightarrow 4} f(x) =$   |  |
| 8. $f(-1) =$                          | 16. $f(4) =$                          |  |

Note that the function is continuous at  $x = 4$  and hence

$$\lim_{x \rightarrow 4} f(x) = \lim_{x \rightarrow 4^-} f(x) = \lim_{x \rightarrow 4^+} f(x) = f(4) = -1.$$

## EXERCISES

For the function  $f$  graphed below, find the following:



1.  $\lim_{x \rightarrow -5^-} f(x) =$
2.  $\lim_{x \rightarrow -5^+} f(x) =$
3.  $\lim_{x \rightarrow -5} f(x) =$
4.  $f(-5) =$
5.  $\lim_{x \rightarrow -2^-} f(x) =$
6.  $\lim_{x \rightarrow -2^+} f(x) =$
7.  $\lim_{x \rightarrow -2} f(x) =$
8.  $f(-2) =$
9.  $\lim_{x \rightarrow 0^-} f(x) =$
10.  $\lim_{x \rightarrow 0^+} f(x) =$
11.  $\lim_{x \rightarrow 0} f(x) =$
12.  $f(0) =$
13.  $\lim_{x \rightarrow 1^-} f(x) =$
14.  $\lim_{x \rightarrow 1^+} f(x) =$
15.  $\lim_{x \rightarrow 1} f(x) =$
16.  $f(1) =$
17.  $\lim_{x \rightarrow 3^-} f(x) =$
18.  $\lim_{x \rightarrow 3^+} f(x) =$
19.  $\lim_{x \rightarrow 3} f(x) =$
20.  $f(3) =$
21.  $\lim_{x \rightarrow 4^-} f(x) =$
22.  $\lim_{x \rightarrow 4^+} f(x) =$
23.  $\lim_{x \rightarrow 4} f(x) =$
24.  $f(4) =$
25.  $\lim_{x \rightarrow 5^-} f(x) =$
26.  $\lim_{x \rightarrow 5^+} f(x) =$
27.  $\lim_{x \rightarrow 5} f(x) =$
28.  $f(5) =$
29. List the value(s) of  $x$  at which  $f$  is discontinuous.

**ANSWERS**

- |                   |                    |                              |
|-------------------|--------------------|------------------------------|
| 1. 2              | 11. 6              | 21. 1                        |
| 2. 2              | 12. 6              | 22. $-4$                     |
| 3. 2              | 13. 7              | 23. Does not exist           |
| 4. 1              | 14. 4              | 24. 1                        |
| 5. $-1$           | 15. Does not exist | 25. $-3$                     |
| 6. 4              | 16. 7              | 26. 1                        |
| 7. Does not exist | 17. 2              | 27. Does not exist           |
| 8. 2              | 18. 2              | 28. 1                        |
| 9. 6              | 19. 2              | 29. $x = -5, -2, 1, 3, 4, 5$ |
| 10. 6             | 20. Undefined      |                              |